Student Number:



2024

TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

Mathematics Extension 1

General Instructions

- Reading time 10 minutes
- Working time 2 hours
- Write using black pen.
- NESA approved calculators may be used.
- A reference sheet is provided.
- In section II, show relevant mathematical reasoning and/or calculations.

Total marks:	Se	Section I – 10 marks	
70	•	Attempt questions 1 - 10	
	•	Allow about 15 minutes for this section.	

Section II – 60 marks

- Attempt questions 11 16.
- Allow about 1 hour and 45 minutes for this section.
- Start each question on a new page.

Section I

10 marks Attempt questions 1 - 10 Allow about 15 minutes for this section.

Use the multiple-choice answer sheet for questions 1-10

1. Given that

$$\sin A = \frac{5}{13}$$
 and $\sin B = \frac{8}{17}$, find the value of $\sin (A + B)$. A and B are acute angles.
A. $-\frac{107}{140}$
B. $-\frac{21}{221}$
C. $\frac{107}{140}$
D. $\frac{171}{221}$

- 2. The angle between the vectors u = -2i + 6j and v = 4i 2j is closest to:
 - A. 45°
 - B. 60°
 - C. 135°
 - D. 120°

3. What is the exact value of
$$\int_{0}^{8} \cos^{2}x \, dx$$
?

π

A.
$$\frac{\pi - 2\sqrt{2}}{8}$$

B.
$$\frac{\pi - 2\sqrt{2}}{16}$$

C.
$$\frac{\pi + 2\sqrt{2}}{8}$$

D.
$$\frac{\pi + 2\sqrt{2}}{16}$$

- 4. What is the value of $\int_{0}^{1} x^{2} \sqrt{1 x^{3}} dx$, using the substitution $u = 1 x^{3}$? A. $-\frac{2}{9}$ B. $-\frac{1}{9}$ C. $\frac{1}{9}$ D. $\frac{2}{9}$
- A course regulation requires that the same number of students achieve each grade from A to E where possible.
 What is the smallest number of students required to ensure that at least one particular grade is awarded 7 times?
 - A. 30
 - B. 31
 - C. 35
 - D. 36
- 6. A circular disc is heated so that the face is increasing in area at a constant rate of 10 cm^2 /s. What is the rate at which the radius of the disc is increasing when the radius is 6 cm?
 - A. 0.26 cm/s
 - B. 0.27cm/s
 - C. 3.76 cm/s
 - D. 3.77 cm/s

- 7. What is the multiplicity of the root x = 1 of the equation
 - $f(x) = 3x^5 5x^4 + 5x 3$? A. 1 B. 2 C. 3 D. 4

8. What is the inverse function of $f(x) = e^{x^3}$?

- A. $f^{-1}(x) = 3e^x$
- B. $f^{-1}(x) = 3\ln x$
- C. $f^{-1}(x) = \sqrt[3]{\ln x}$
- D. $f^{-1}(x) = \sqrt{3 \ln x}$
- 9. A curve is represented by the following parametric equations:

$$x = 2 \cos \theta$$
, $y = 2 \sin \theta$

Which of the following is the cartesian equation of the curve?

- A. x + y = 2
- B. x + y = 4
- C. $x^2 + y^2 = 2$
- D. $x^2 + y^2 = 4$

- 10. The polynomial $f(x) = 2x^2 + kx + 4$ can be expressed as f(x) = (x 2)g(x) + 6. Which of the following is the correct expression for g(x)?
 - A. 2*x* 1
 - B. 2x + 1
 - C. 2*x* 3
 - D. 2x + 3

Section II

60 marks Attempt all questions Allow about 1 hour and 45 minutes for this section.

Start each question on a new page in the answer booklet provided. Your responses should include relevant mathematical reasoning and/or calculations. Extra writing paper is available on request.

Question 11 (10 marks)

a. Solve
$$\frac{1}{2x-1} - x > 0$$
 [3]

b. The polynomial $4x^3 - 12x^2 + 5x + 6 = 0$ has roots α , β and γ .

Find α , β and γ given that one of the roots is the sum of the other two. [3]

c. (i) Write
$$3\cos x - \sqrt{3}\sin x$$
 in the form $R\cos(x + \alpha)$. [2]

(ii) Hence, solve
$$3\cos x - \sqrt{3}\sin x = \sqrt{3}$$
 for $0 \le x \le 2\pi$. [2]

Question 12 (10 marks)

a. Given that
$$\underbrace{u}_{\infty} = 2\underbrace{i}_{\infty} + 3\underbrace{j}_{\infty}$$
 and $\underbrace{v}_{\infty} = -2\underbrace{i}_{\infty} + 4\underbrace{j}_{\infty}$, find $\operatorname{proj}_{\underbrace{u}}\underbrace{v}_{\infty}$. [2]

b. Use the substitution
$$t = \tan \frac{x}{2}$$
 to solve

$$\cos x - 3\sin x + 3 = 0$$
 for $0 \le x \le 2\pi$. [4]

c. Use the substitution
$$u = \sin x$$
 to find $\int -\cos x \sin^2 x \, dx$. [2]

d. In how many ways can 8 people be placed in groups of 2? [2]

Question 13 (10 marks)

- a. Factorise $P(x) = 4x^3 3x^2 25x 6$ [3]
- b. Prove that $\sec A (1 \sin A)(\sec A + \tan A) = 1$ [2]

c. Use mathematical Induction to prove that $3^{3n} + 2^{n+2}$ is divisible by 5 [3] for $n \ge 1$.

d. Find
$$\int \frac{1}{9 + 16x^2} dx$$
 [2]

Question 14 (10 marks)

a. In the diagram below, *OABC* is a parallelogram. $\overrightarrow{OA} = \overrightarrow{a}$ and $\overrightarrow{OC} = \overrightarrow{c}$. *P* is the point on *AB* such that $AP = \frac{1}{4}AB$. 2

Q is the point on OC such that $OQ = \frac{2}{3} OC$.

Find \overrightarrow{PQ} in terms of a_{α} and c_{α} , giving your answer in simplest surd form.



b. Newton's law of cooling states that the rate of change of the temperature θ , of a body at any time *t*, is proportional to the difference in the temperature of the body and the temperature *m*, of the surrounding medium, i.e.

 $\frac{d\theta}{dt} = k(\theta - m)$, where *k* is a constant.

- (i) Show that $\theta = m + Ae^{kt}$ where A is a constant, satisfies this equation. [1]
- (ii) If the temperature of the surrounding air is $40^{\circ}C$ and the temperature of the body drops from $170^{\circ}C$ to $105^{\circ}C$ in 45 minutes, find the temperature of the body in another 90 minutes (to 2 decimal places). [2]
- (iii) Find the time taken for the temperature of the body to drop to $80^{\circ}C$ (to the nearest minute). [2]

c. Find the coefficient of x in the expansion of
$$\left(x + \frac{2}{x^2}\right)^{10}$$
 [2]

[3]

Question 15 (10 marks)

a. David throws a pebble from a height of 2 metres at an angle of θ to the horizontal, with a velocity of 30m/s.



- (i) Show that the expression for the horizontal and vertical displacements at *t* seconds after projection are $x = 30t \cos \theta$ and $y = -5t^2 + 30t \sin \theta + 2$ respectively. [2] (Take g = 10m/s and take the origin to be the ground directly below David)
- (ii) Show that the equation of the path of the particle is: $y = \frac{-x^2}{180} (1 + \tan^2 \theta) + x \tan \theta + 2$ [2]
- (iii) If David manages to hit a target at point *T*, which is 10 metres away horizontally and 6 metres high, find the two possible angles of projection. [2]
- b. For the function $y = 2 \sin^{-1} (2x 1) + \frac{\pi}{2}$ (i) Find the domain and range. [2]
 - (ii) Sketch the curve, clearly showing the coordinates of the endpoints. [2]

Question 16 (10 marks)

a. Solve the equation $\sin 3x - \sin x + \cos 2x = 0$ for $0 \le x \le 2\pi$. [3]

b. (i)) Prove that	$8\cos^4 x = 3 + 4\cos 2x + \cos 4x \; .$	[2]
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(ii) Hence, find the volume generated when the area bounded by the curve $y = \cos^2 x$, the *x*-axis and x = 0 and $x = \frac{\pi}{4}$ [2]

is rotated about the *x*-axis.

- c. A committee of 5 is to be chosen from six men and seven women.
 - (i) How many committees are possible if there are no restrictions? [1]
 (ii) How many committees are possible if there are more women than men? [2]

End of Examination

Mathematics Assessment Solutions
Girraween High School

 Task: Trial HSC Extension 1

 Year: 2024

 Suggested Solutions

 Question 1 2: C 3. D 4. D 5. B C. B T. C S. C 4. D 10. B

 1. A and B Uic in
$$\Theta$$
1
 B

 Sin (A + B) = Sin Acos B + CosA Sin B A
 B

 $= \frac{12}{15} \times 15 + \frac{12}{15} \times \frac{3}{17}$
 B

 $= \frac{12}{15} \times 15 + \frac{12}{15} \times \frac{3}{17}$
 B

 $= \frac{12}{12}$
 D

 Z · Cos $\Theta = \underbrace{U \cdot Y}_{I \otimes I \otimes I}$
 D

 $= \frac{(-2) \times 4 + 6 \times (-2)}{\sqrt{Ivo} \times 120}$
 D

 $= -\frac{20}{20\sqrt{2}}$
 D

 $\Theta = 135^{\circ}$
 CC]





Suggested Solutions
Question 6

$$\frac{dA}{dt} = 10 \text{ cm}^{2}/\text{s} ; \frac{dr}{dt} = ?; r = 6 ; A = \pi r^{2}$$

$$\frac{dA}{dt} = \frac{dA}{dr} \times \frac{dr}{dt}$$

$$10 = 2 \pi r \times \frac{dr}{dt}$$

$$10 = 2 \pi r \times \frac{dr}{dt}$$

$$\frac{dr}{dt} = \frac{10}{2\pi r}$$

$$= \frac{10}{2\pi \kappa 6} \quad (\text{when } r = 6)$$

$$= 0 \cdot 27 \text{ cm}/\text{s} \quad [B]$$

$$\frac{\text{Question 7}}{\text{P(x)} = 15x^{5} - 5x^{4} + 5x - 3 ; P(1) = 0$$

$$P'(x) = 15x^{4} - 20x^{3} + 5 ; P'(1) = 0$$

$$P''(x) = 160x^{2} - 120x ; P(1) = 0$$

$$P''(x) = 150x^{2} - 120x ; P(1) = 60 \neq 0$$

$$\therefore \text{ Multiplicity} = 3 \quad [C]$$
Marker's Feedback

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Page <u>5</u>

Suggested Solutions

$$G_{decision 10}$$

$$f(x) = (x - 2)g(x) + b = 2)f(2) = b (Remainder theorem)$$

$$f(z) = 2xz^{2} + 2k + 4 = 4$$

$$12 + 2k = 6$$

$$2k = -6$$

$$k = -3$$

$$2x^{2} - 3x + 4 = (x - 2)g(x) + 4$$

$$2x^{2} - 3x - 2 = (x - 2)g(x)$$

$$(x - 2)(2x + 1) = (x - 2)g(x)$$

$$\vdots, g(x) = 2x + 1$$

$$[B]$$
Marker's Feedback

Suggested Solutions Question \\ a) 1 -x >0, 2+2 Colne $\frac{1}{2x-1} = x$ $2\pi^2 - \pi = 1$ 222-2-1=0 (2x+1)(x-1)=0 $\chi = -\frac{1}{2}, 1$ $\begin{array}{c} \chi = -\frac{1}{2}, \\ \downarrow \\ \downarrow \\ -\frac{1}{2} \\ -\frac{1}{2} \\ 1 \\ \end{array}$ Test 22 = -1 Test 21=0 Test 21=0.8 ļ $-1 -0 > 0 \qquad -0.8 > 0$ -1 2(0.8) - 1 $\frac{1}{2(-1)^{-1}}$ -(-1)>0 X Test n=2 Solution : $\frac{1}{2(2)-1}$ - 2 >0 $x < -\frac{1}{2}, \frac{1}{2} < x < 1$ ļ X 3 Marker's Feedback

Page 7(A)

Suggested Solutions	
Question 11	
a)	
2x - 1, $2 + 2$	
2×1	
r. 2	
(X(2x-1))	
(7) (7) (7) (7) (-1)	
	1
2	-
$\chi(2)(-1) \leq 2(1-1)$	
2	
$\chi(2n-1) - (2n-1) < 0$	
($)$ $($ $)$ $)$ $()$ $($	
(2,1-1) $(2,1-1) = 1$ $(2,1-1) = 1$	
	1
(2,1-1)(2,1-2)(-2)(-1) < 0	7
$(2_{1}-1)(2_{1}+1)(x-1)<0$	
Ay 4	
	l
	1
Solution , x < - 4 4 X X I	3
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Suggested Solutions
Question II C)
i)
$$3 \cos x - \sqrt{3} \sin x \equiv R \cos (x + d)$$

 $= R \cos x \cos d - R \sin x \sin d$
Equating like terms,
 $R \cos d = 3 - 0$; $R \sin d = (3 - 2)$
 $\operatorname{squaring}$ and $\operatorname{odding} 0$ and (2)
 $R^2 (\sin^2 d + \cos^2 d) = 12$
 $R = 2\sqrt{3}$ ($R > 0$)
 $\sin d = \frac{1}{2}$; $\cos d = \frac{\sqrt{3}}{2}$ = $3 \operatorname{d} \operatorname{in} \varphi_1$
 $\therefore d = \frac{\pi}{6}$
 $1 \times 3\cos x - \sqrt{3}\sin x = 2\sqrt{3} \cos (x + \pi_6)$ [2]
II) $3 \cos x - \sqrt{3}\sin x = \sqrt{3}$
 $2\sqrt{3} \cos (x + \pi_6) = \sqrt{3}$
 $\cos (x + \pi_6) = \frac{1}{2}$
 $x + \pi_6 = \pi_3 \text{ or } 5\pi_2$
 $x = \pi_6, 3\pi_2$ [2]
Marker's Feedback



Suggested Solutions
Question 12
b) $t = \tan \frac{x}{2}$
$\cos x - 3\sin x + 3 = 0$
$\frac{1-t^2}{1+t^2} - 3\left(\frac{2t}{1+t^2}\right) + 3 = 0$
$1-t^2 - 6t + 3(1+t^2) = 0$
$1-t^2 - 6t + 3 + 3t^2 = 0$
$2t^2 - 6t + 4 = 0$
$t^2 - 3t + 2 = 0$
(t-1)(t-2)=0
t = 1, 2
ie. $\tan \frac{2}{2} = 1$ or $\tan \frac{2}{2} = 2$
$\frac{2}{2} = \frac{1}{4}$ $\frac{2}{2} = 1.107$ $\chi = 2.21$ (to 2dp) 1
$\mathcal{L} = \frac{1}{2}$
Test for $\chi = \Pi$ $\therefore \chi = \Pi_{z, z, z_1}$
65 11 - 33/ 11 +3 7
$= -1 + 3 \neq 0$
Marker's Feedback

Page _____

Suggested Solutions Question 12 $\int -\omega s \times s \sin \varkappa dx , U = s \ln x$ 9 du = cos x dx $= -\int u^{3/2} du$ = $-\frac{u^{5/2}}{5/2} + c$ 1 $= -\frac{2}{5} \sin^{\frac{5}{2}} x + c$ | 2 8(2×6C2×4C2×2C2 d) -1 41 = 105 ーン Marker's Feedback

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Suggested Solutions
Question 13
a)
$$f(x) = 4 x^{3} - 3x^{2} - 25 x - 6$$

Try: Factors $q - 6 = \pm 1, \pm 2, \pm 3, \pm 6$
 $f(-2) = 4(-2)^{3} - 3(-2)^{2} - 25(-2) - 6$
 $= 0$
 $\therefore (x+2)$ is a factor
 $\frac{4x^{2} - 11x - 3}{7x + 2}$
 $\frac{4x^{2} - 25x}{- 11x^{2} - 25x} = 6$
 $\frac{-4x^{3} + 8x^{2}}{- 3x - 6}$
 $\frac{-3x - 6}{-3x - 6}$
 $\therefore f(x) = (x + 2) (4x^{2} - 11x - 3)$
 $= (x + 2) (2 - 3) (4x + 1)$ [
Marker's Feedback
[3]

Suggested Solutions Question 13 b) SecA (1-SINA) (SecA + tan A) = 1 LNS = Sec A (I-SINA) (Sec A + tan A) $= \frac{1}{\log A} \left(1 - \sin A \right) \left(\frac{1}{\log A} + \frac{\sin A}{\cos A} \right)$ 1 $= \frac{1}{\cos A} \left(1 - \sin A\right) \frac{1}{\cos A} \left(1 + \sin A\right)$ $= \frac{1}{\cos^{2}A} (1 - \sin^{2}A)$ $= \frac{1}{\cos^{2}A} (\cos^{2}A)$ 1 = 1 = RHS 2 Marker's Feedback

Suggested Solutions
Question 13
(c)
$$3^{3n} + 2^{n+2}$$
 is divisible by 5 ; $n \ge 1$
Step 1 : Show true for $n=1$
 $3^3 + 2^3 = 35$ which is divisible by 5.
Step 2 : Assume true for $n=k$ for integer $k > 0$
i.e. $3^{3k} + 2^{k+2} = 5M$; M is a positive integer
Step 3 : Prove true for $n=kt$:
 $1e \cdot 3^{3k} + 2^{k+3} = 5N$; N is a positive integer
 $1e \cdot 3^{3k} + 2^{k+3} = 5N$; N is a positive integer
 $1e \cdot 3^{3k} + 2^{k+3} = 5N$; N is a positive integer
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 $1e \cdot 3^{3k} + 2^{k+2} = 5N$; N is a positive integer
 $135M - 27 \times 2^{k+2} + 2 \times 2^{k+2} = 135M - 25 \times 2^{k+2} = 135M - 25 \times 2^{k+2} = 5(27M - 5 \times 2^{k+2}) = 5N$; If true for $n=k$, then also frue for $n=k$;
 $1e \cdot 5N$; If true for $n=k$, then also frue for $n=k$;
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 $1e \cdot 5N$; If true for $n=k$; then also frue for $n=k$;
 $1e \cdot 5N$; If true for $n=k$; $n=k$; $3M$; If $n\geq 1$; $3M$; 3

1

Suggested Solutions
Question 13

$$\frac{d}{d} \int \frac{1}{(q+1)b_{z}^{2}} dz$$

$$= \int \frac{1}{3^{2} + (q_{x})^{2}} dz$$

$$= \frac{1}{4} \int \frac{4}{3^{2} + (q_{x})^{2}} dz$$

$$= \frac{1}{4} \times \frac{1}{3} + an^{-1} \left(\frac{q_{x}}{3}\right) + c$$

$$= \frac{1}{12} + an^{-1} \left(\frac{4x}{3}\right) + c$$

$$= \frac{1}{12} - an^{-1} \left(\frac{4x}{3}\right) + c$$

$$\boxed[2]$$
Marker's Feedback



Suggested Solutions Question 14 b) i) $b = m + Ae^{kt}$ => Aekt = A-m $\frac{d\theta}{dt} = kAe^{kt}$ = k(Q-m) (since $Ae^{kt} = Q-m$) 1 : 0 = m + Ae^{kt} satisfies the equation. ij $\theta = m + Ae^{kt}$ At +=0, 170 = 40+Ae° : A = 130 $45k = \ln \frac{65}{130}$ 0 = 40+ 130 ekt At t=45 k = -0.0154 45k 105 = 40+ 130e 65 = 130 e 45k $45k \ln e = \ln \frac{65}{130}$ cont --- > P19 **Marker's Feedback**

Suggested Solutions Question 14 b (ii) cont At t= 135 125 k 0 = 40 + 130e 1= = 56.25°C (to 2dp) $0 = 80^{\circ}, t = 7$ 80 = 40+130e kt 1 40 = 130ekt t = In + - k = 76.53 1 = 77 minutes 2 Marker's Feedback

Suggested Solutions Question 14 $\begin{pmatrix} x+2\\ x^2 \end{pmatrix}^{10}$ $T_{k+1} = C_k a^{n-k} b^k$ $= {}^{10}C_{k} \cdot \chi \cdot (2x^{-2})^{k}$ $= {}^{10}C_{1}.2c_{2}k_{2}k_{2}-2k_{2}$ $= \binom{10}{4} \frac{10}{2} - \frac{3}{2}$ 1 coefficient of x => 10-3k=1 k = 3 :. Coefficient of $x = \frac{10}{3} (3.2^3)$ = 960 2 **Marker's Feedback**

Suggested Solutions
Question 15
a) j Initially,

$$\frac{30}{2}$$
 $\frac{1}{9} = 30 \text{ Sin B}$
 $\frac{30}{2}$ $\frac{1}{9} = 30 \text{ Sin B}$
 $\frac{30}{2}$ $\frac{1}{9} = 30 \text{ Sin B}$
 $\frac{30}{2}$ $\frac{1}{2} = 30 \text{ Cos B}$
 $\frac{1}{2} = 0$
 $\frac{1}{2} = -10t + C_1$
When $t = 0$, $\frac{1}{2} = 30 \text{ Sin B}$
 $\frac{1}{2} = 30 \text{ Cos B} + C_2$
 $\frac{1}{2} = -10t + C_1$
When $t = 0$, $\frac{1}{2} = 30 \text{ Sin B}$
 $\frac{1}{2} = 30 \text{ Cos B} + C_2$
 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + C_2$
 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + 2$
 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + 2$
 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + 2$
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 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + 2$
 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + 2$
 $\frac{1}{2} = -5t^2 + 30t \text{ Sin B} + 2$



Suggested Solutions
Question 15
a) (ii)
when
$$\pi = 10^{2}$$
, $y = 6$
 $\therefore 6 = \frac{-10^{2}}{180}$ ($1 + \tan^{2}\theta$) + $10 \tan \theta + 2$
 $6 = -\frac{5}{9}$ ($1 + \tan^{2}\theta$) + $10 \tan \theta + 2$
 $54 = -5 - 5\tan^{2}\theta + 90\tan\theta + 18$
 $5\tan^{2}\theta - 90\tan\theta + 41 = 0$
 $\tan^{2}\theta = 90 \pm \sqrt{90^{2} - 4x5 \times 45}$
 10
 $= \frac{90 \pm \sqrt{3280}}{10}$
 $\theta = 87^{\circ}, 25^{\circ}$ (θ is acute)
Marker's Feedback

Suggested Solutions Question 15 y = 2 sin -1 (2x -1) + # b) $\frac{Y-\frac{\pi}{2}}{2} = Sin^{-1}(2n-1)$ Domain : -1 < 2x-1 < 1 0 5 2 51 1 Range: $\frac{y-\frac{\pi}{2}}{\frac{z}{2}} \leq \frac{\pi}{2}$ -π ≤ ^y-^π/₂ ≤ π 1 / 2 **Marker's Feedback**



Suggested Solutions
Question 16
(a) Sin 3x - Sin K + Los 2x =0;
$$0 \le x \le 2\pi$$

Sin $(2x + x) - Sin (2\pi - x) + Los 2x = 0$
 $2 \cos 2x \sin x + \cos 2x = 0$
 $2 \cos 2x \sin x + \cos 2x = 0$
 $\cos 2x (2\sin x + 1) = 0$
 $\cos 2x (2\sin x + 1) = 0$
 $\cos 2x = 0$; $0 \le 2x \le 4\pi$
 $2x = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}$
 $x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$
 $x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$
 $x = \frac{\pi}{4}, \frac{3\pi}{5}, \frac{5\pi}{4}, \frac{7\pi}{4}, \frac{7\pi}{4}$
 $x = \frac{\pi}{4}, \frac{3\pi}{5}, \frac{5\pi}{4}, \frac{7\pi}{4}, \frac{7\pi}{6}, \frac{11\pi}{6}$
 $x = \frac{\pi}{4}, \frac{3\pi}{5}, \frac{5\pi}{5}, \frac{7\pi}{5}, \frac{7\pi}{6}, \frac{11\pi}{6}$
Marker's Feedback

Suggested Solutions
Question 16
b) j)
$$\Re \cos^4 x = 3 + 4 \cos 2x + \cos 4x$$

LMS = $\Re \cos^4 x$
= $2 (2 \cos^2 x)^2$
= $2 (1 + \cos 2x)^2$
= $2 (1 + 2 \cos 2x + \cos^2 2x)$
= $2 [1 + 2 \cos 2x + \cos^2 2x]$
= $2 [1 + 2 \cos 2x + 1 + \cos 4x]$
= $2 + 4 \cos 2x + 1 + \cos 4x$
= $3 + 4 \cos 2x + \cos 4x$
= 8 Hs .
[2]
Marker's Feedback

Suggested Solutions
Question 16
b (ii)

$$V = \pi \int_{0}^{4} \cos s^{4} \times dx$$

$$= \pi \int_{0}^{4} \frac{1}{8} (3 + 4\cos 2x + \cos 4x) dx$$

$$= \frac{\pi}{8} \left[3x + 2\sin 2x + \frac{1}{4}\sin 4x \right]_{0}^{4}$$

$$= \frac{\pi}{8} \left[3(\frac{\pi}{4}) + 2\sin (\frac{\pi}{2}) + \frac{1}{4}\sin \pi \right] - 0$$

$$V = \frac{\pi}{8} \left[\frac{3\pi}{4} + 2 \right] u^{3}$$
[2]
Marker's Feedback

Suggested Solutions
Question 1/2
C. (1) ¹³ C₅ = 1287 [1]
(ij) More Women than men

$$\Rightarrow 5W$$
: ⁷C₅ = 21
 $\Rightarrow 4W_{1}M$: ⁷C₄ × ⁶C₁ = 210
 $\Rightarrow 3W_{1}2M$: ⁷C₃ × ⁶C₂ = 525
Total = 21 + 210 + 525]
= 756
[2]
Marker's Feedback